

# Motion Planning Networks

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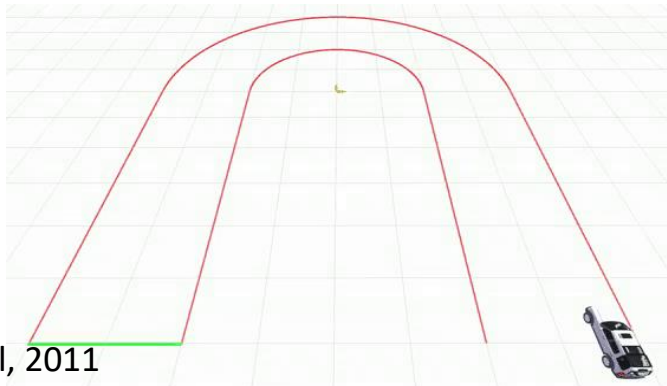
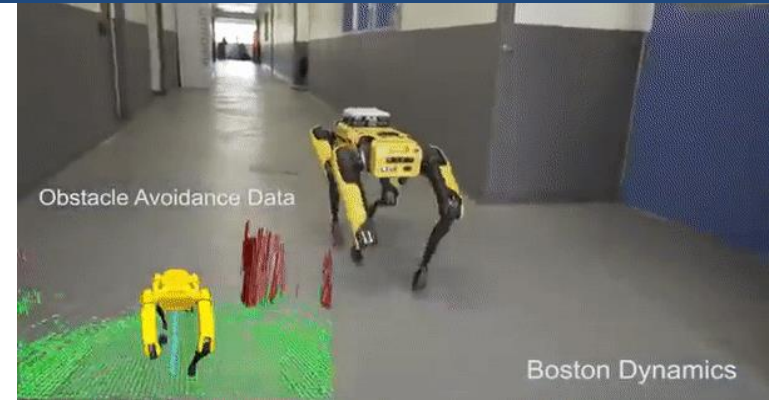
University of California, San Diego

[qureshiahmed.github.io](https://qureshiahmed.github.io)

# Motion Planning

**Find a path that satisfies all constraints between the given start and goal configurations.**

- Collision Avoidance
- Dynamics
- Kinematics (e.g., end-effector)

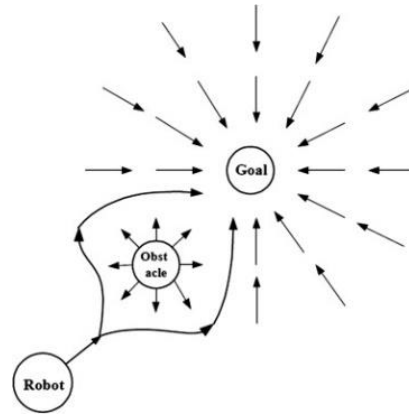


Karaman et. al, 2011

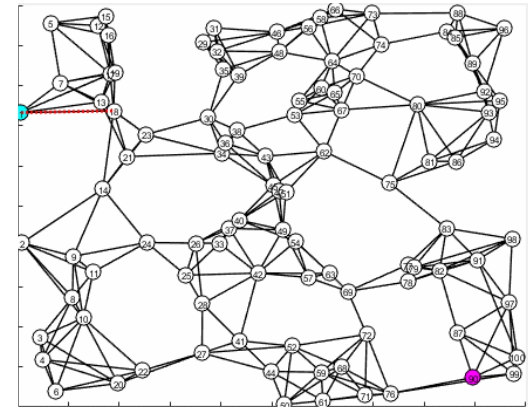


# Common Strategies

Resolution  
Complete  
Methods

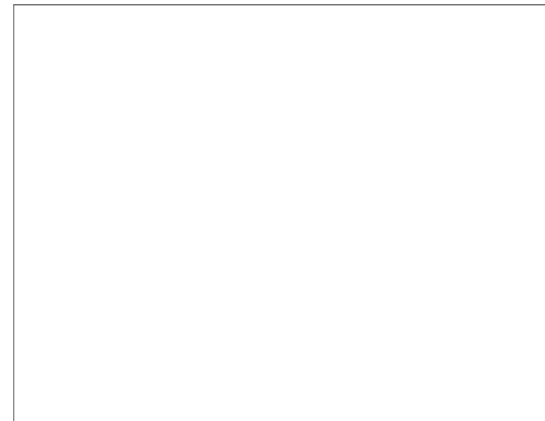


*Artificial Potential Fields (Khatib, 86'), Cell  
Decomposition (Chazelle, 87')*



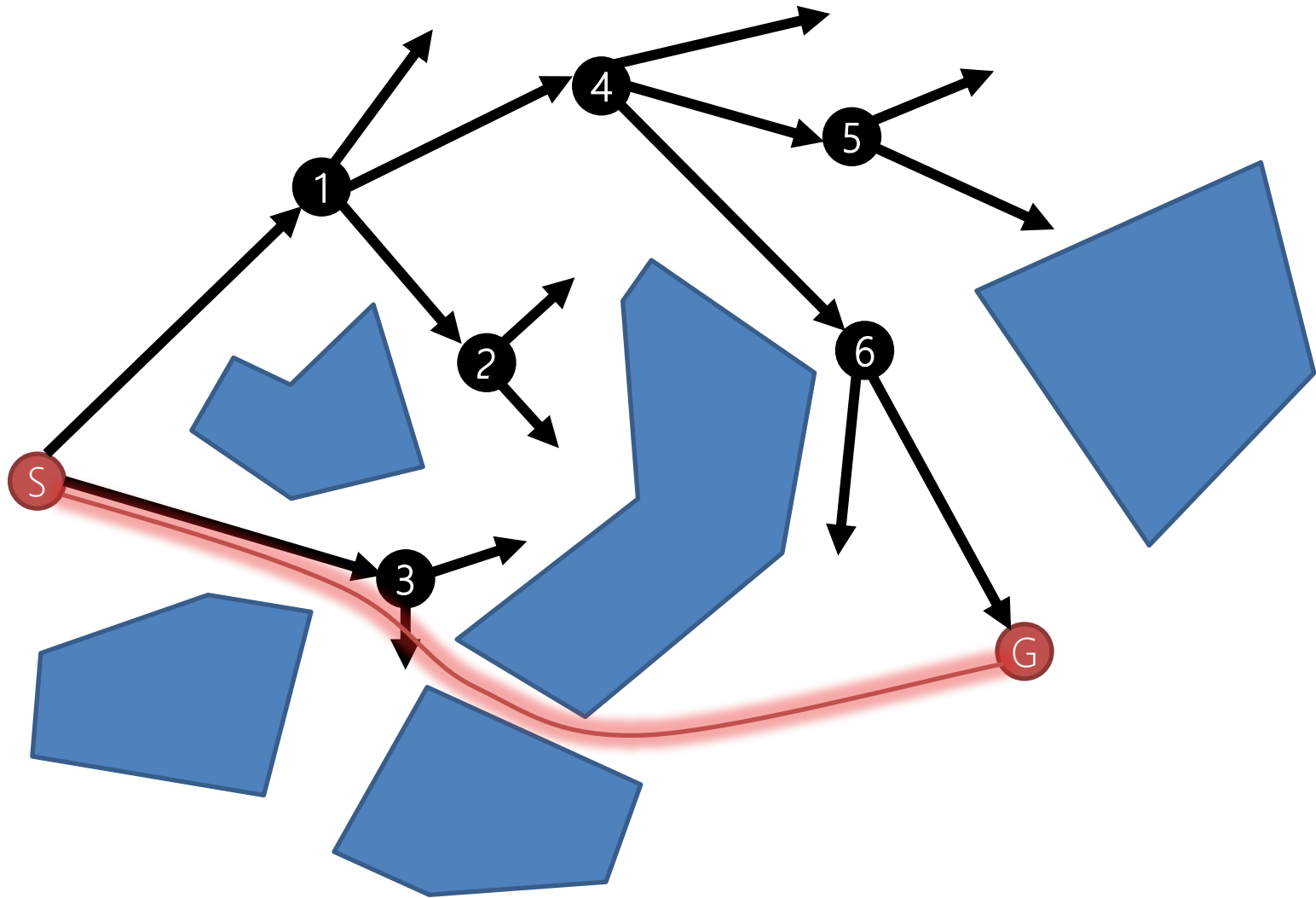
*Visibility Graphs (Lozano-Perez, 79')  
Probabilistic Roadmaps (Kavraki, 96')*

Sample-based  
Planners

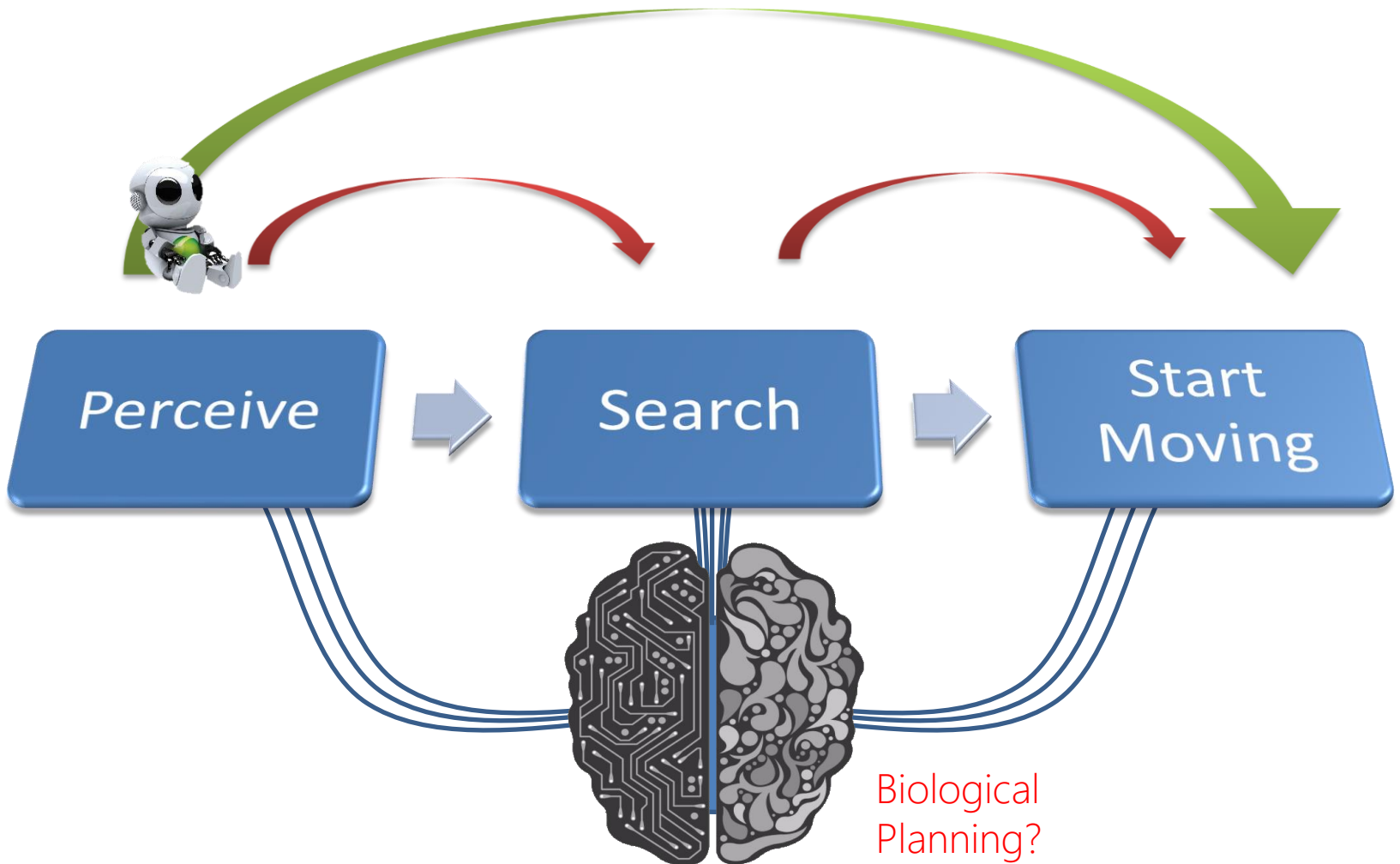


*RRT (LaValle, Kuffner, 98'), RRT\* (Karaman, 2011)*

# Motion Planning



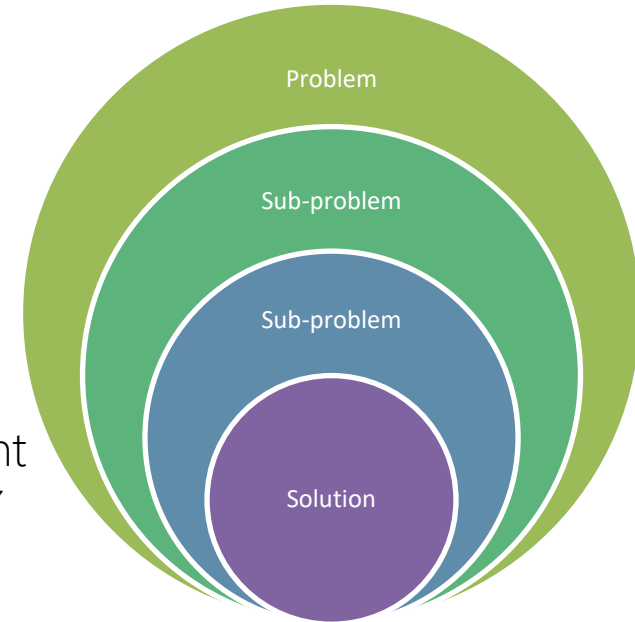
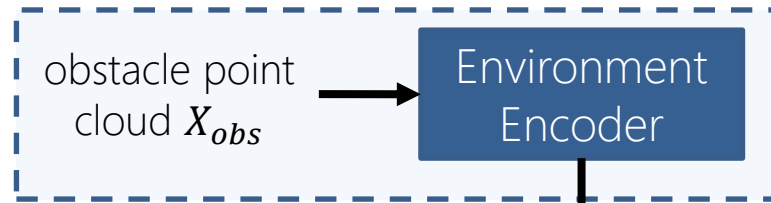
# Sequence in Robot Thinking



# Neural Motion Planning

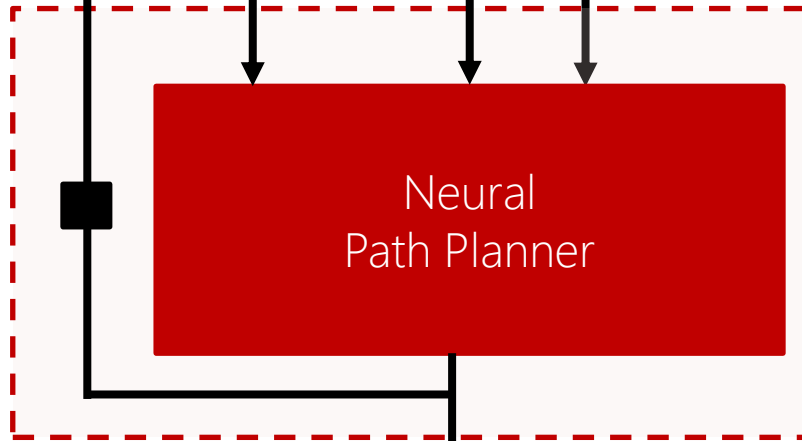
- Motion Planning Networks (MPNet)

## *Environment Encoder*



current  $c_k$       goal  $c_g$       environment encoding  $Z$

## *Neural Planner*

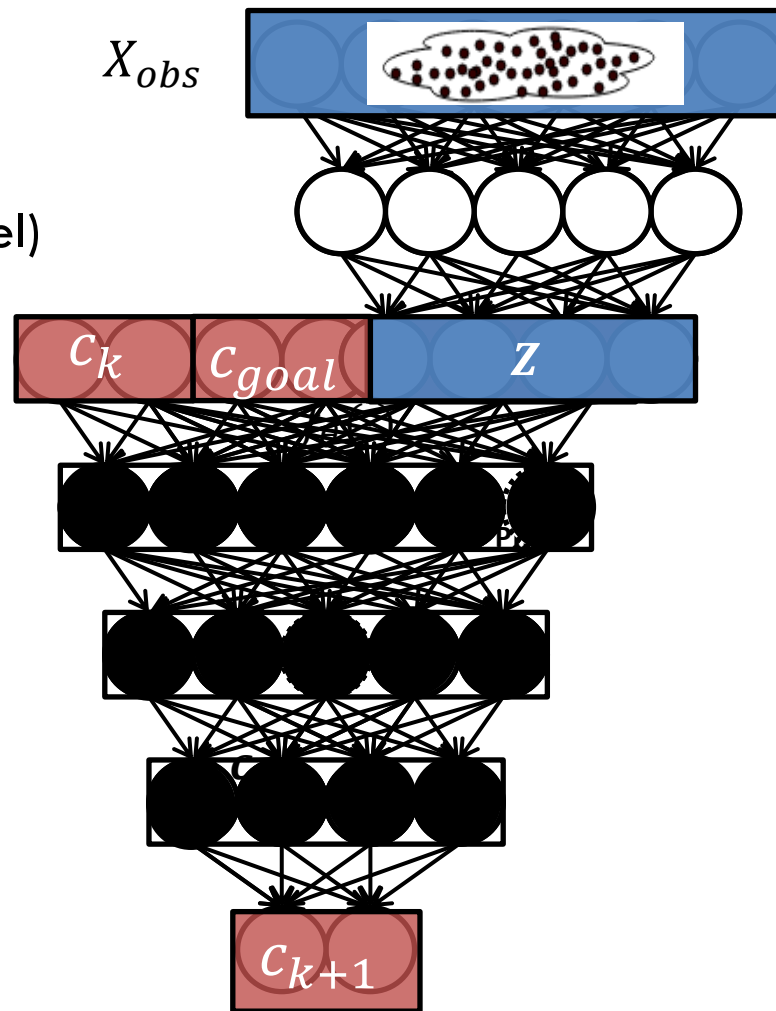


Next configuration  $c_{k+1}$

# MPNet: Motion Planning Networks

## Encoder Network (Enet):

- Input: obstacles point cloud  $x_{obs} \in \mathbb{R}^d$
- Output: Embedding  $Z \in \mathbb{R}^m$
- 3D CNN (Preprocess point-cloud to voxel)
- Feed forward neural network



## Planning Network (Pnet):

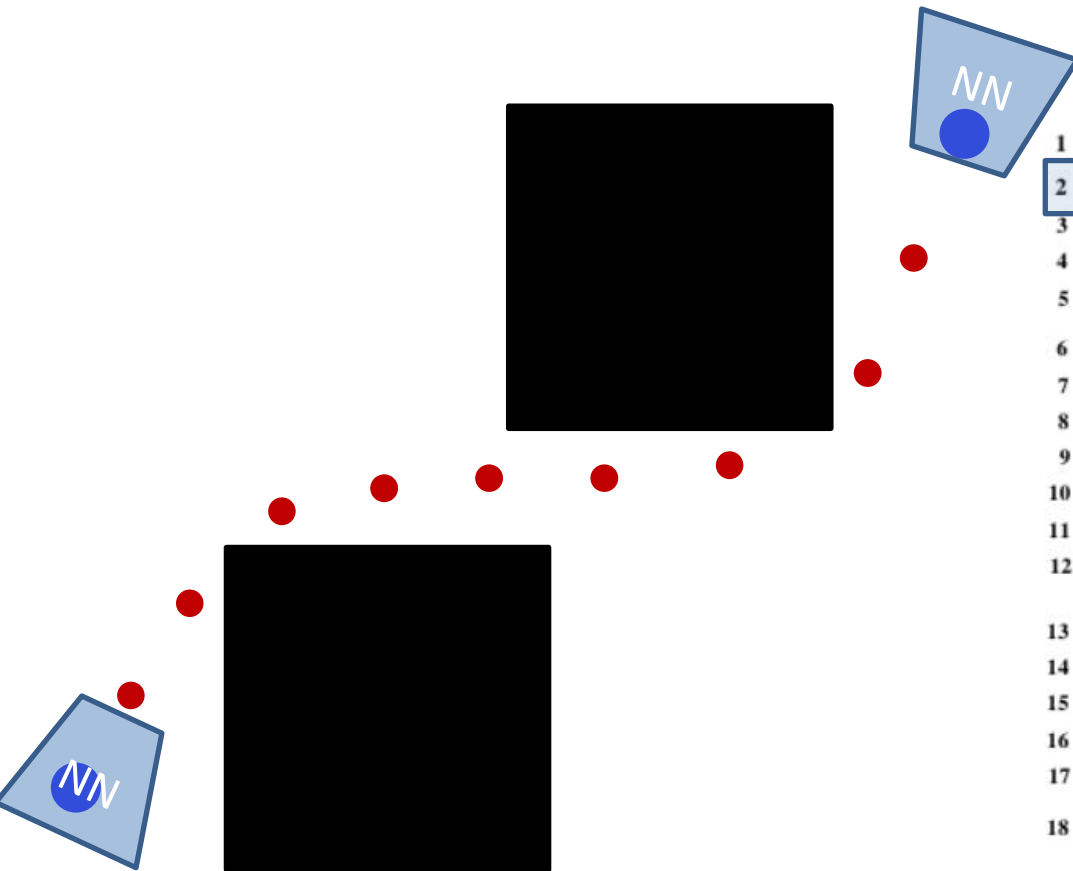
- Input:  $Z, c_t, c_T$
- Output:  $\hat{c}_{t+1} \leftarrow \text{PNet}(c_t, c_T, Z)$
- Stochastic feed-forward neural network

## Recursive Planning Algorithm:

- End-to-end paths or informed samples
- Worst-case theoretical guarantees

# MPNet: Recursive Bidirectional Neural Planning

- Find critical states between given start and goal using MPNet.
- Create a coarse plan.



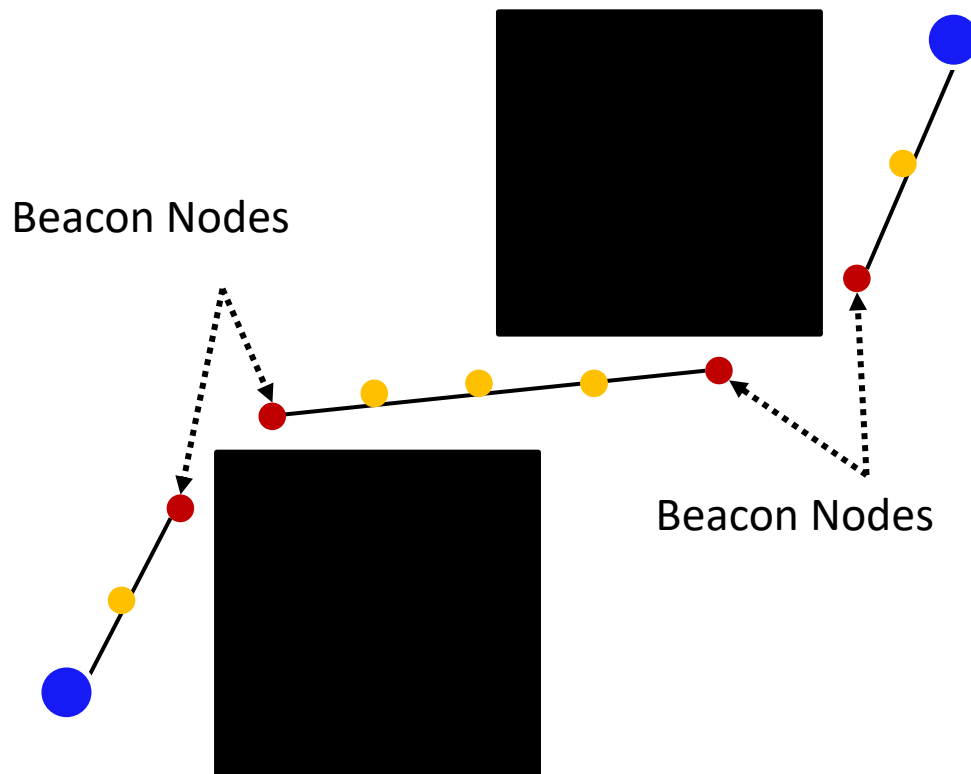
```
1  $Z \leftarrow \text{Enet}(x_{\text{obs}})$ 
2  $\sigma \leftarrow \text{BNP}(c_{\text{init}}, c_{\text{goal}}, Z)$  // BidirectionalNeuralPlanner
3  $\sigma \leftarrow \text{LazyStatesContraction}(\sigma)$ 
4 if  $\text{IsFeasible}(\sigma)$  then
5   return  $\sigma$ 
6 else
7    $p = 0$  // Set replanner to use BNP
8   for  $i \leftarrow 0$  to  $N_r$  do
9      $\sigma \leftarrow \text{Replan}(\sigma, Z, p)$  // NeuralReplanning
10     $\sigma \leftarrow \text{LazyStatesContraction}(\sigma)$ 
11    if  $\text{IsFeasible}(\sigma)$  then
12      return  $\sigma$ 
13   $p = 1$  // Set replanner to use OraclePlanner
14   $\sigma \leftarrow \text{Replan}(\sigma, Z, p)$  // HybridReplanning
15   $\sigma \leftarrow \text{LazyStatesContraction}(\sigma)$ 
16  if  $\text{IsFeasible}(\sigma)$  then
17    return  $\sigma$ 
18  return  $\emptyset$ 
```





# MPNet: Recursive Bidirectional Neural Planning

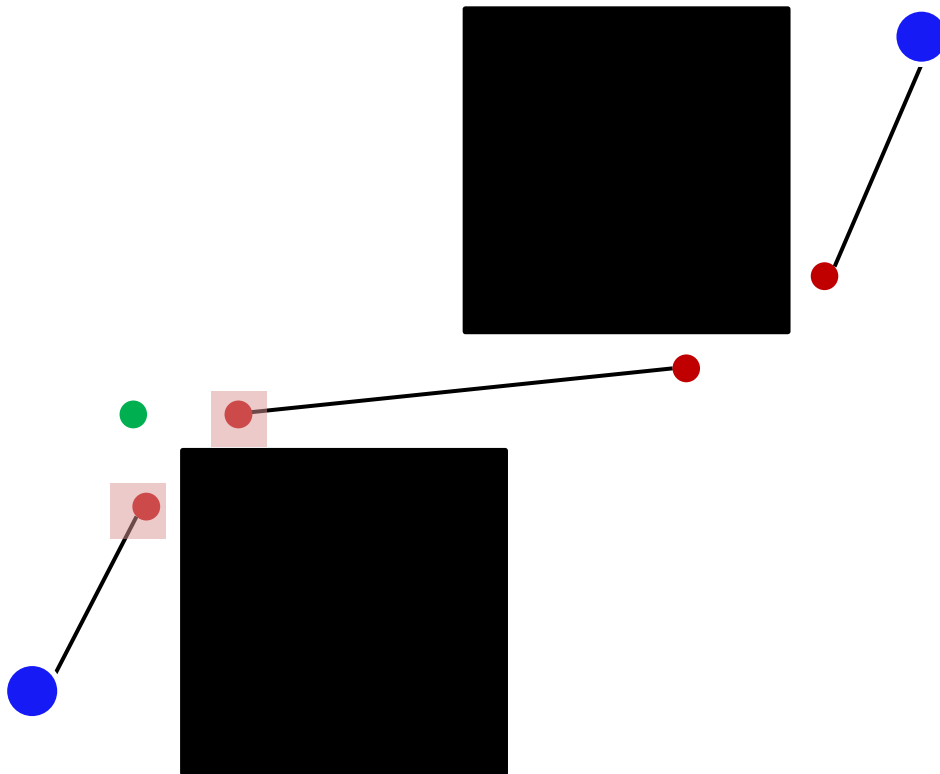
- Remove redundant states (branch-and-bound).
- Identify beacon states.



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1  $Z \leftarrow \text{Enet}(x_{\text{obs}})$ 
2  $\sigma \leftarrow \text{BNP}(c_{\text{init}}, c_{\text{goal}}, Z)$  // BidirectionalNeuralPlanner
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```

# MPNet: Recursive Bidirectional Neural Planning

- Replan between beacon states with MPNet (Divide and conquer approach)



```
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2  $\sigma \leftarrow \text{BNP}(c_{\text{init}}, c_{\text{goal}}, Z)$  // BidirectionalNeuralPlanner
3  $\sigma \leftarrow \text{LazyStatesContraction}(\sigma)$ 
4 if  $\text{IsFeasible}(\sigma)$  then
5   return  $\sigma$ 
6 else
7    $p = 0$  // Set replanner to use BNP
8   for  $i \leftarrow 0$  to  $N$ , do
9      $\sigma \leftarrow \text{Replan}(\sigma, Z, p)$  // NeuralReplanning
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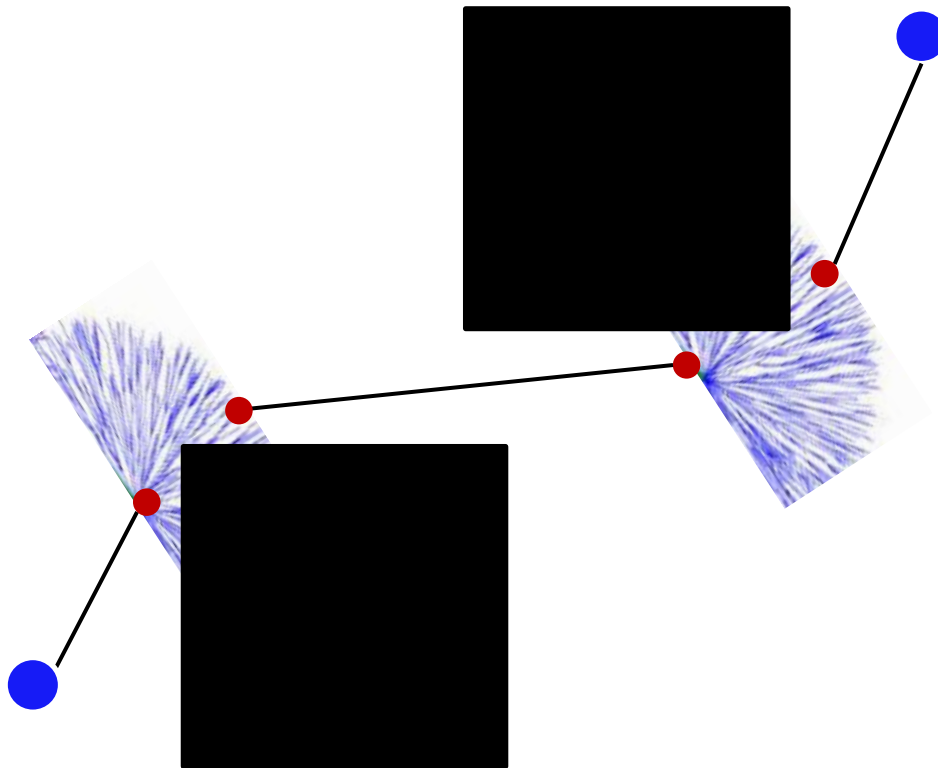






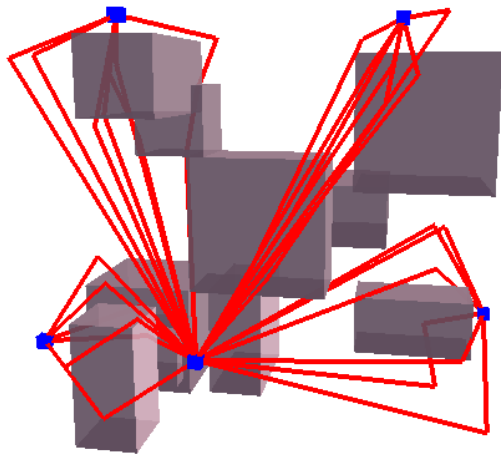
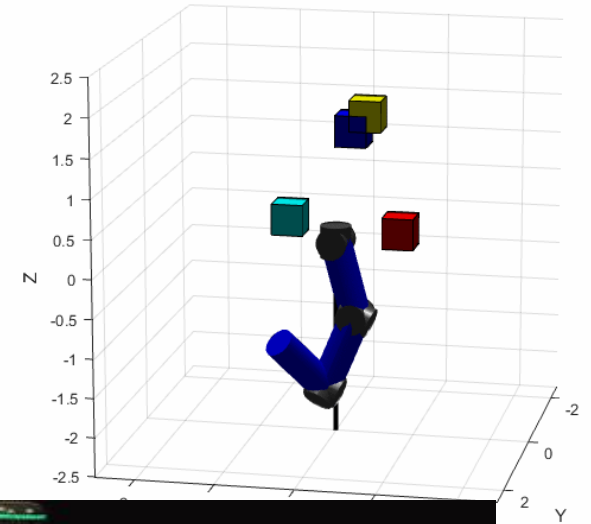
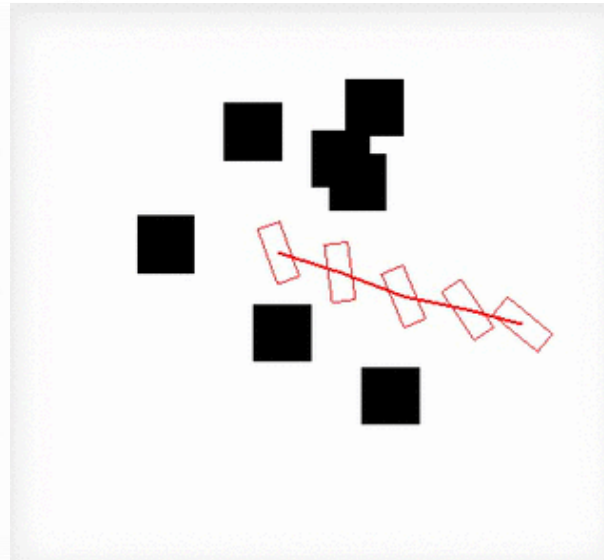
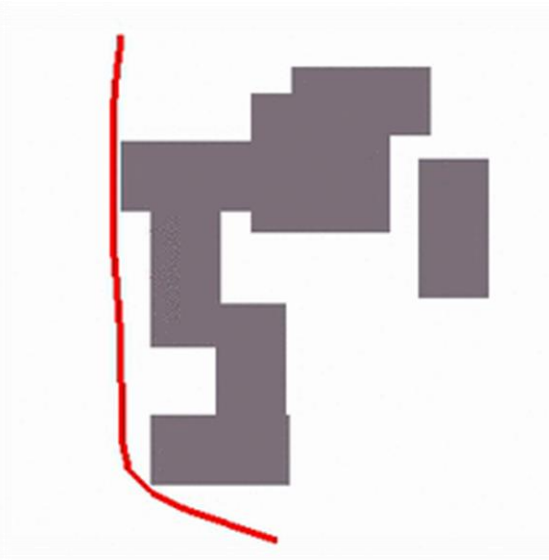
# MPNet: Recursive Bidirectional Neural Planning

- **Hybrid replanning:** Combines MPNet with classical planners.
  - Outsource a segment of a planning problem to a classical planner.



```
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4 if IsFeasible( $\sigma$ ) then
5   return  $\sigma$ 
6 else
7    $p = 0$  // Set replanner to use BNP
8   for  $i \leftarrow 0$  to  $N_r$  do
9      $\sigma \leftarrow \text{Replan}(\sigma, Z, p)$  // NeuralReplanning
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18 return  $\emptyset$ 
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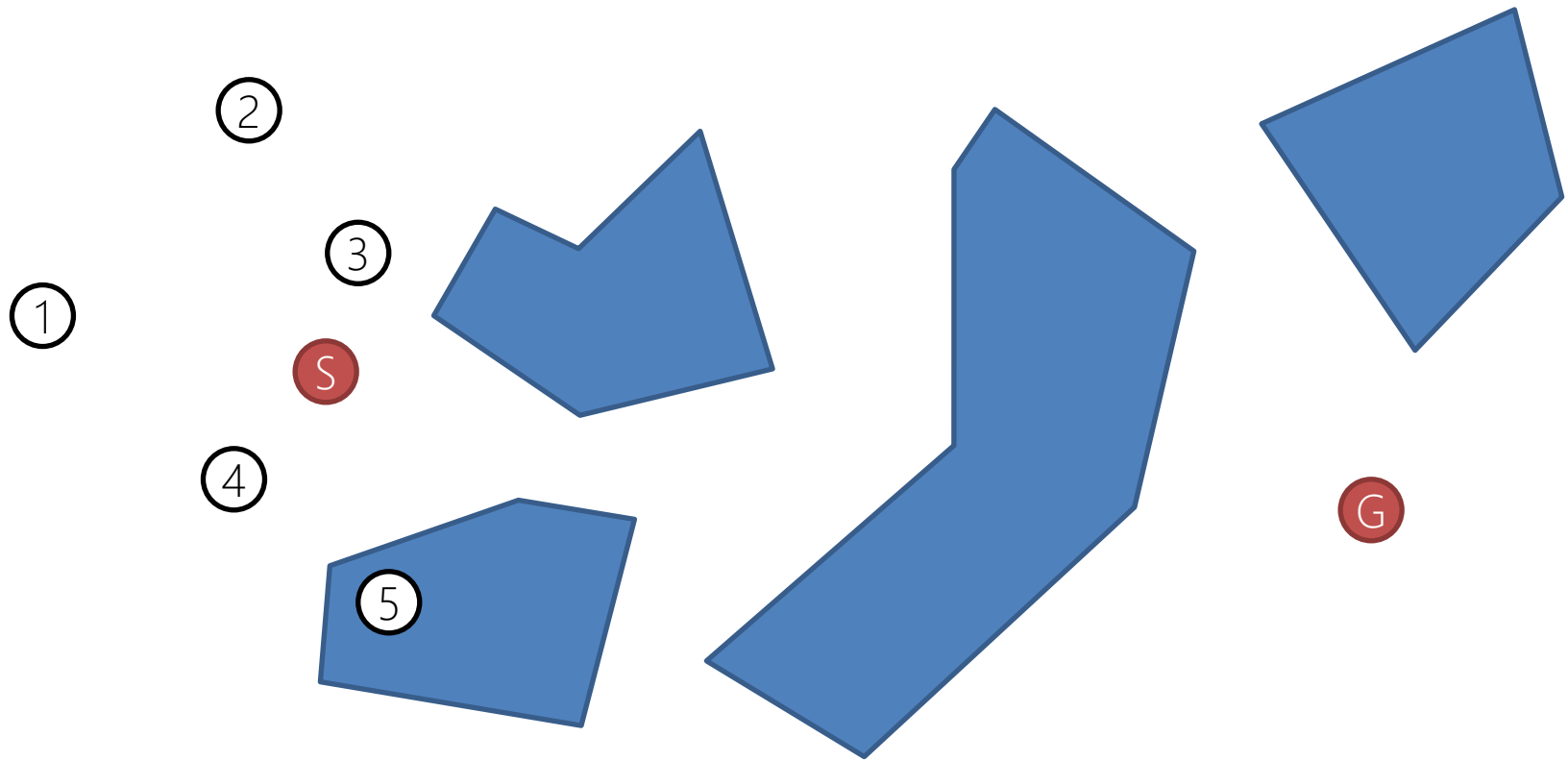
# Visualizations





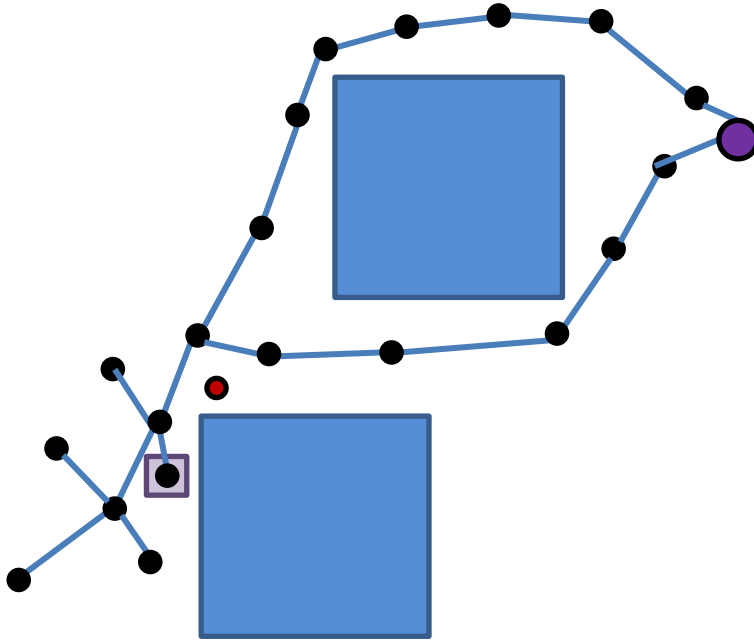
# Informed Sampling

But what if we wanted to use this not to *find the solution* but make *informed choices*?



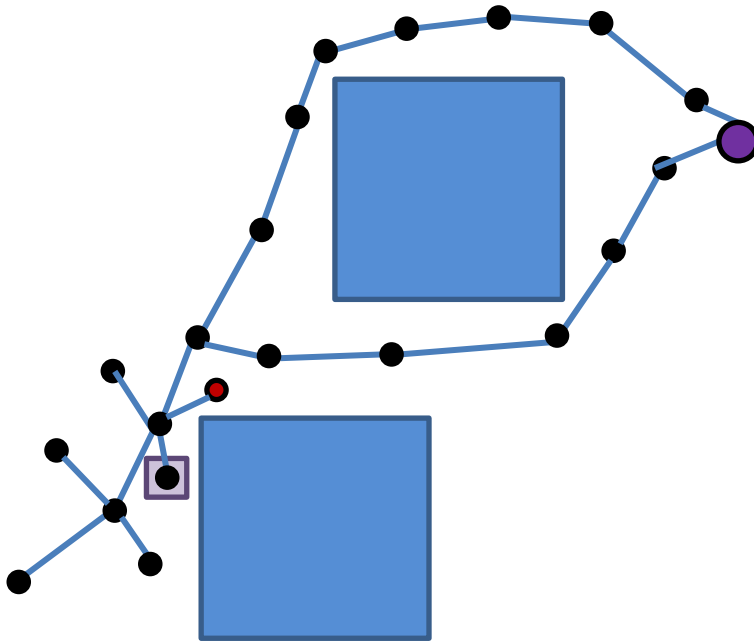


# MPNet: Informed Sampling



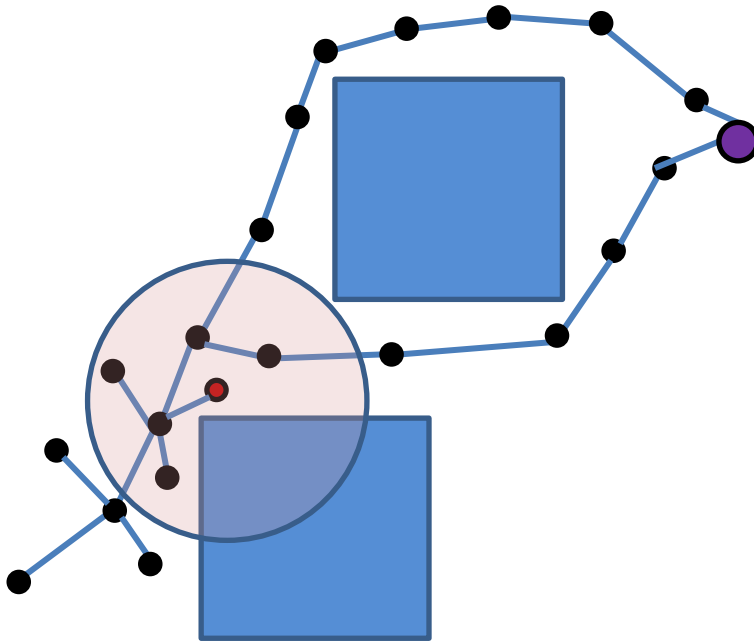
```
1 Initialize  $T \leftarrow \text{SMP}(c_{\text{init}}, c_{\text{goal}}, \mathcal{X}_{\text{obs}})$ 
2  $c_{\text{rand}} \leftarrow c_{\text{init}}$ 
3  $Z \leftarrow \text{Enet}(x_{\text{obs}})$ 
4 for  $i \leftarrow 0$  to  $n$  do
5   if  $i < N_{\text{smp}}$  then
6      $c_{\text{rand}} \leftarrow \text{MPNet}(Z, c_{\text{rand}}, c_{\text{goal}})$ 
7   else
8      $c_{\text{rand}} \leftarrow \text{RandomSampler}()$ 
9      $c_{\text{nearest}} \leftarrow \text{Nearest}(c_{\text{rand}}, T)$ 
10    if  $\text{Steer}(c_{\text{nearest}}, c_{\text{rand}})$  then
11       $C_{\text{near}} \leftarrow \text{Near}(c_{\text{rand}}, T)$ 
12       $T \leftarrow \text{Rewire}(T, C_{\text{near}}, c_{\text{rand}})$ 
13    if  $c_{\text{rand}} \in c_{\text{goal}}$  then
14       $c_{\text{rand}} \leftarrow c_{\text{init}}$ 
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# MPNet: Informed Sampling



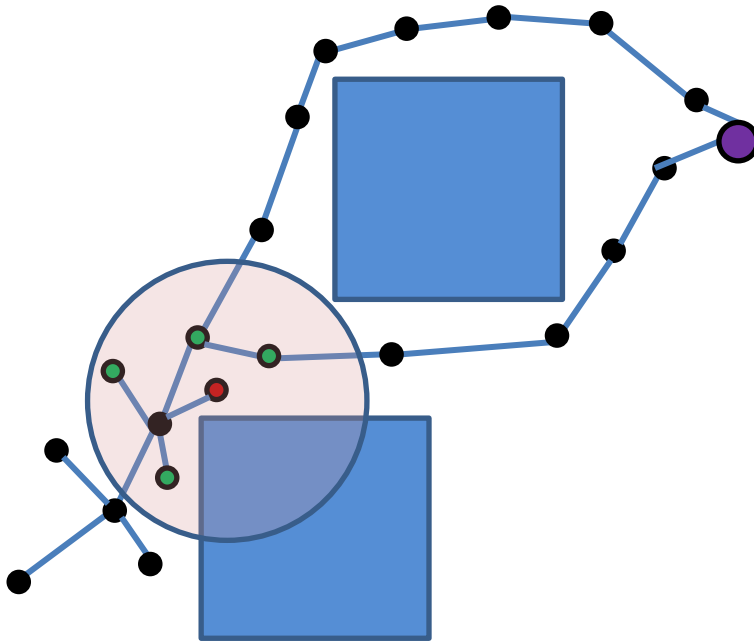
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# MPNet: Informed Sampling



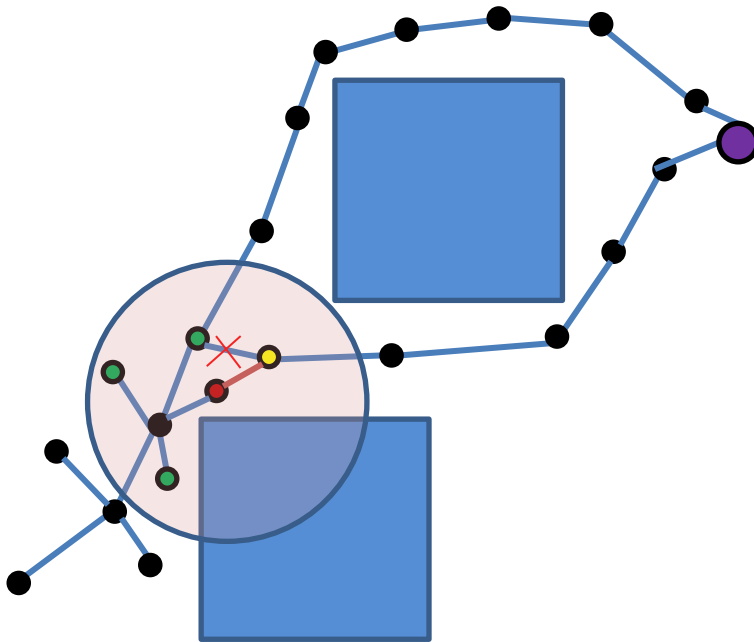
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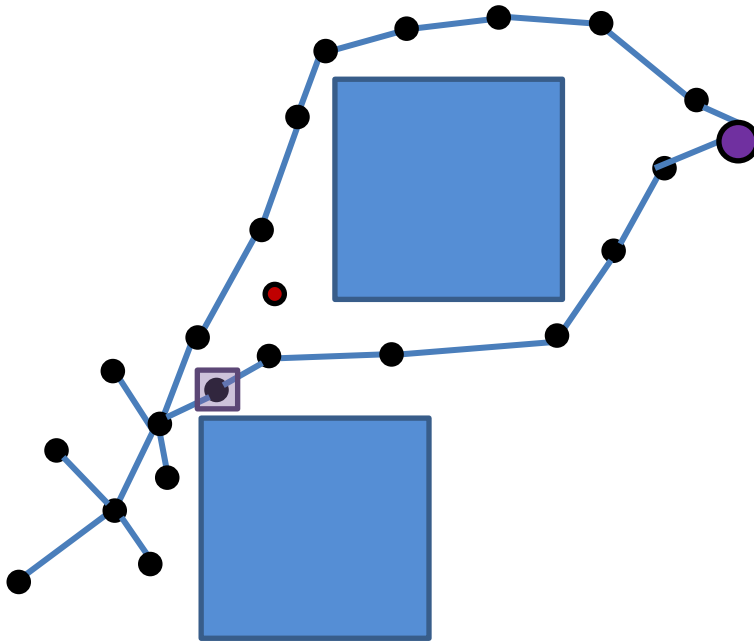


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# Informed Sampling

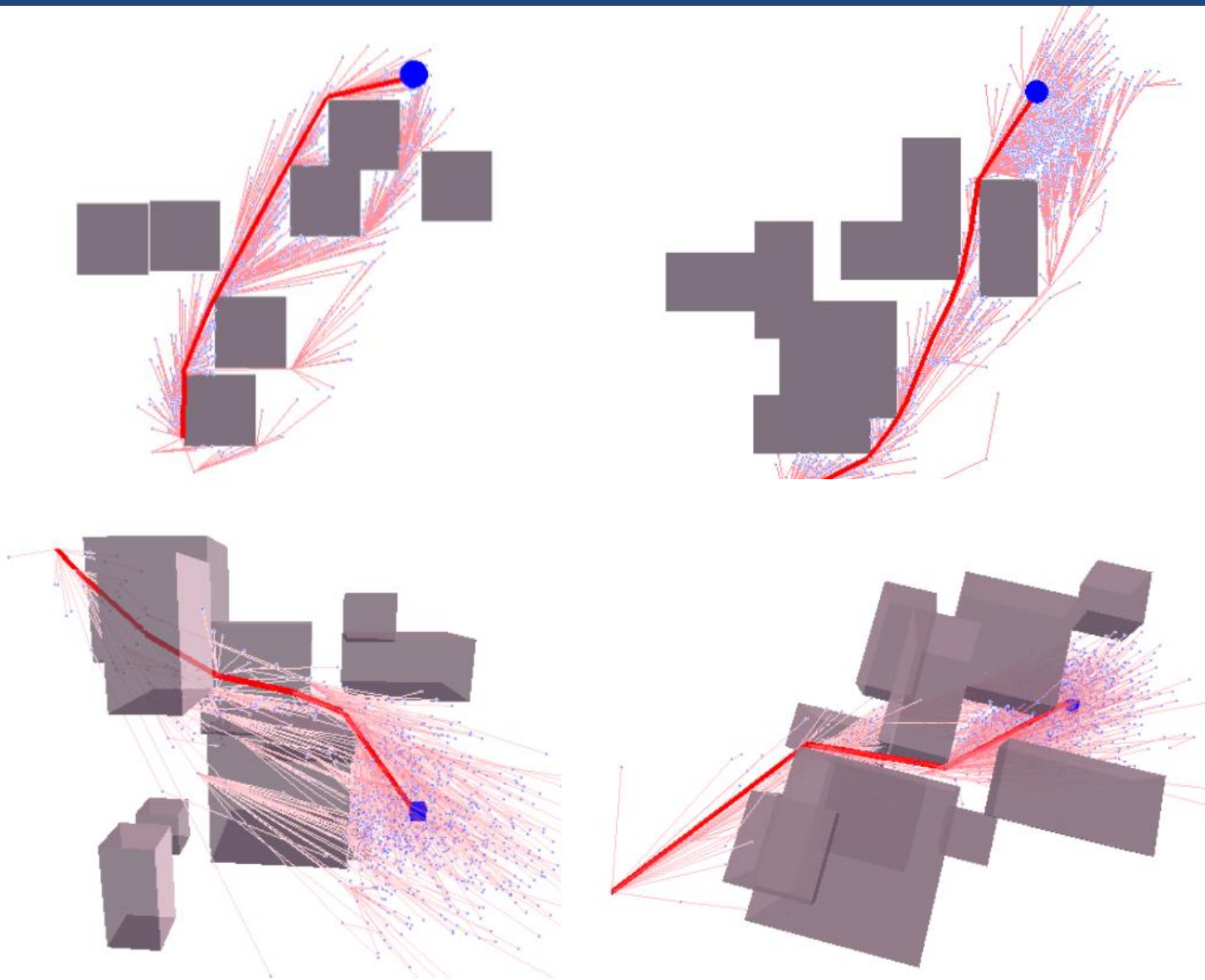


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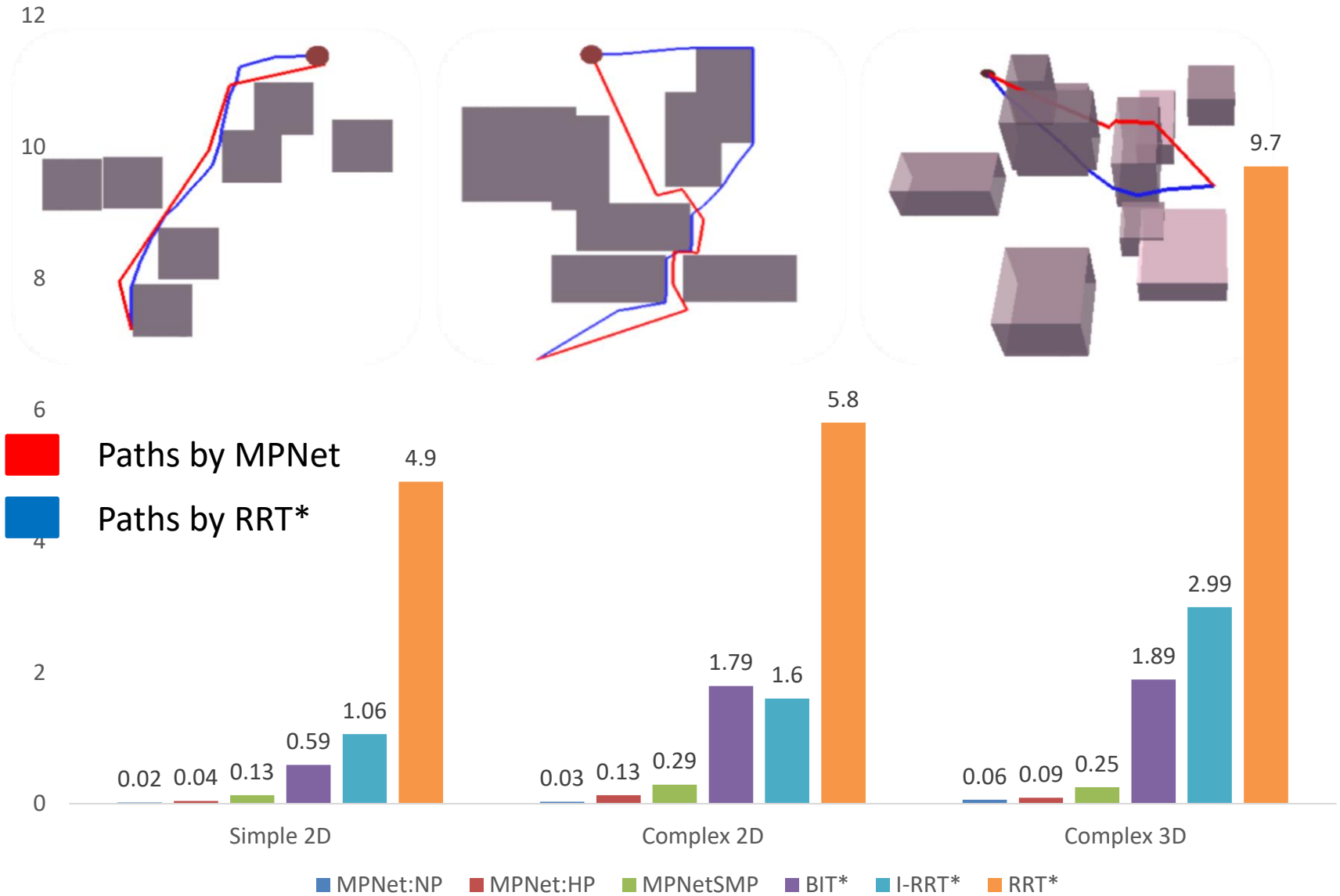




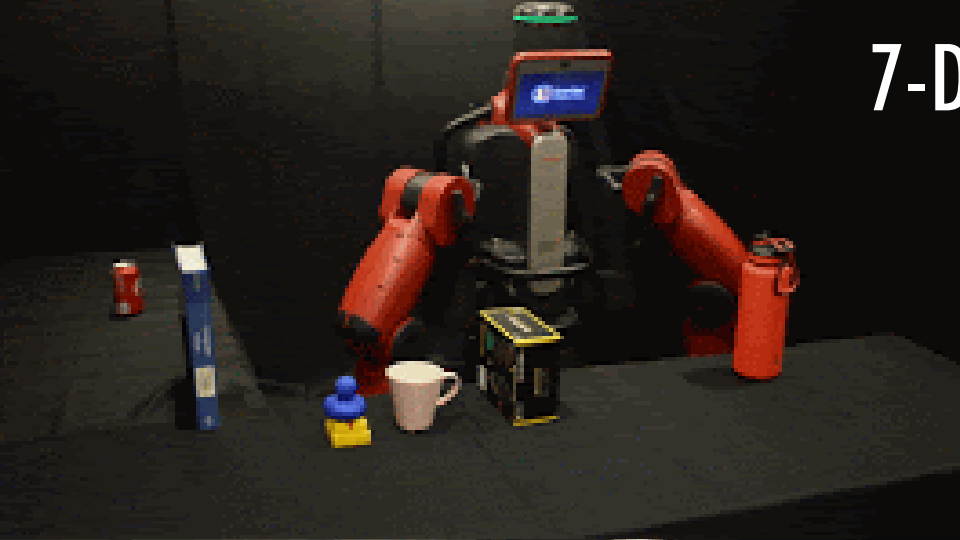
# Informed Sampling Visualization



# Results



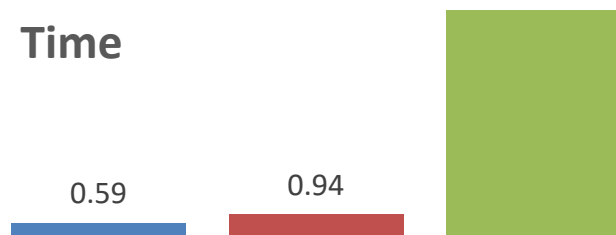
# 7-DOF



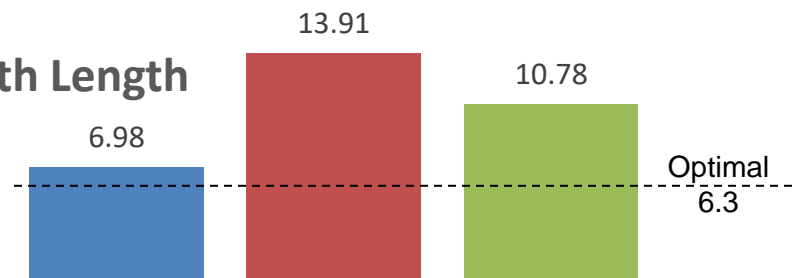
■ MPNet ■ BIT\* (Initial) ■ BIT\* (40% of MPNet Cost)

■ MPNet ■ BIT\* (Initial) ■ BIT\* (40% of MPNet Cost)

### Time



### Path Length



# Summary of Results

## **End-to-end collision-free paths with minimal-to-no branching**

- Significantly faster than state of art in challenging environments
- Significantly less variance in time-to-completion.
- Near-optimal path length

## **Decompose planning problems into sub-problems.**

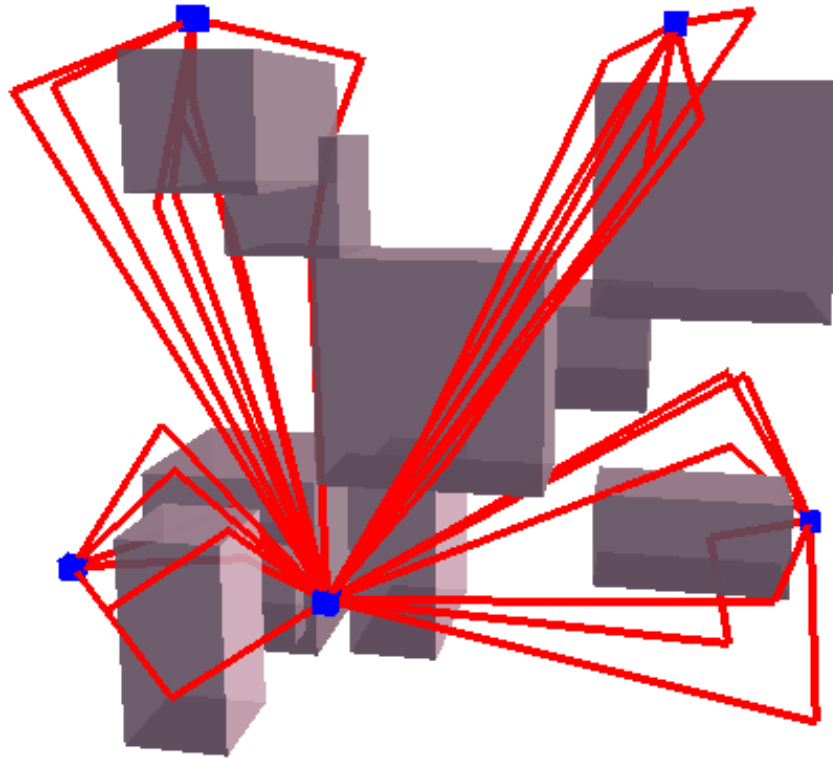
- Allows easy integration with standard planners.
  - retains computational benefits with completeness guarantees.

## **Can learn from streaming data**

- Can actively ask for demonstrations only when needed.
- Reduced data for learning
- minimizes catastrophic forgetting

## **Validated on variety of environments**

- Seen and unseen environments from 2 to 7DOF.



## MPNET: EXTENSIONS

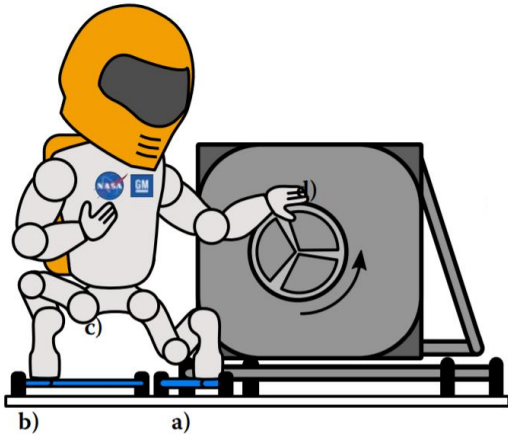


# Motion Planning

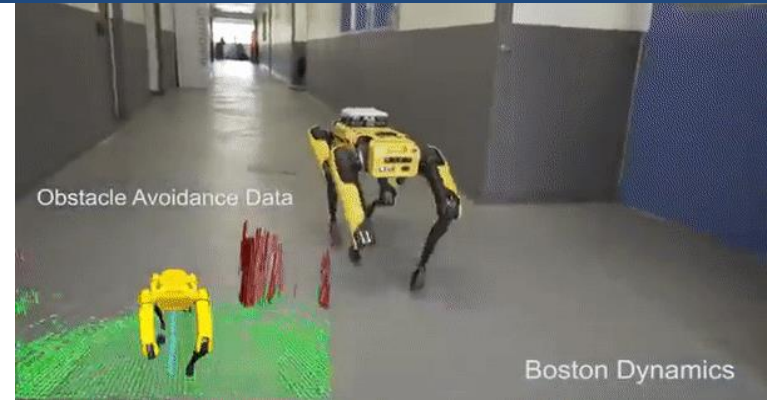
**Find a path that satisfies all constraints between the given start and goal configurations.**

- Collision Avoidance

- Kinematics (e.g., end-effector)
- Dynamics

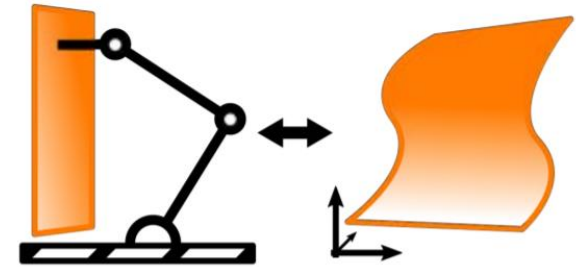


Kingston et. al, 2018



# Motion Planning under Kinematic Constraints

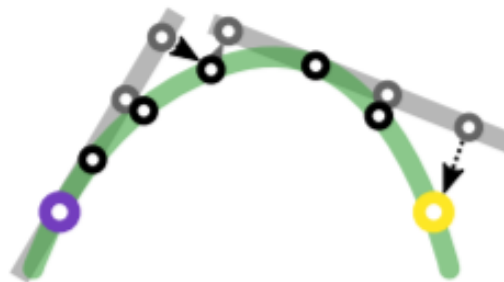
- Bi-RRT & Constraint-adherence approaches
  - CBiRRT: Projection [1]
  - Atlas-RRT: Atlas [2]
  - TB-RRT: Tangent Bundle [3]



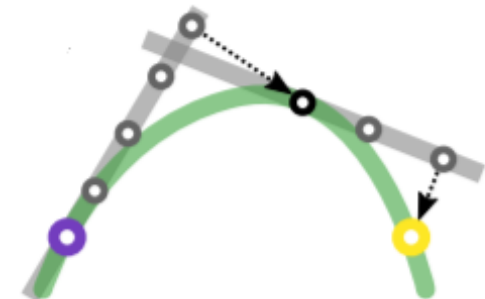
Kingston et. al, 2018, 2019



Projection



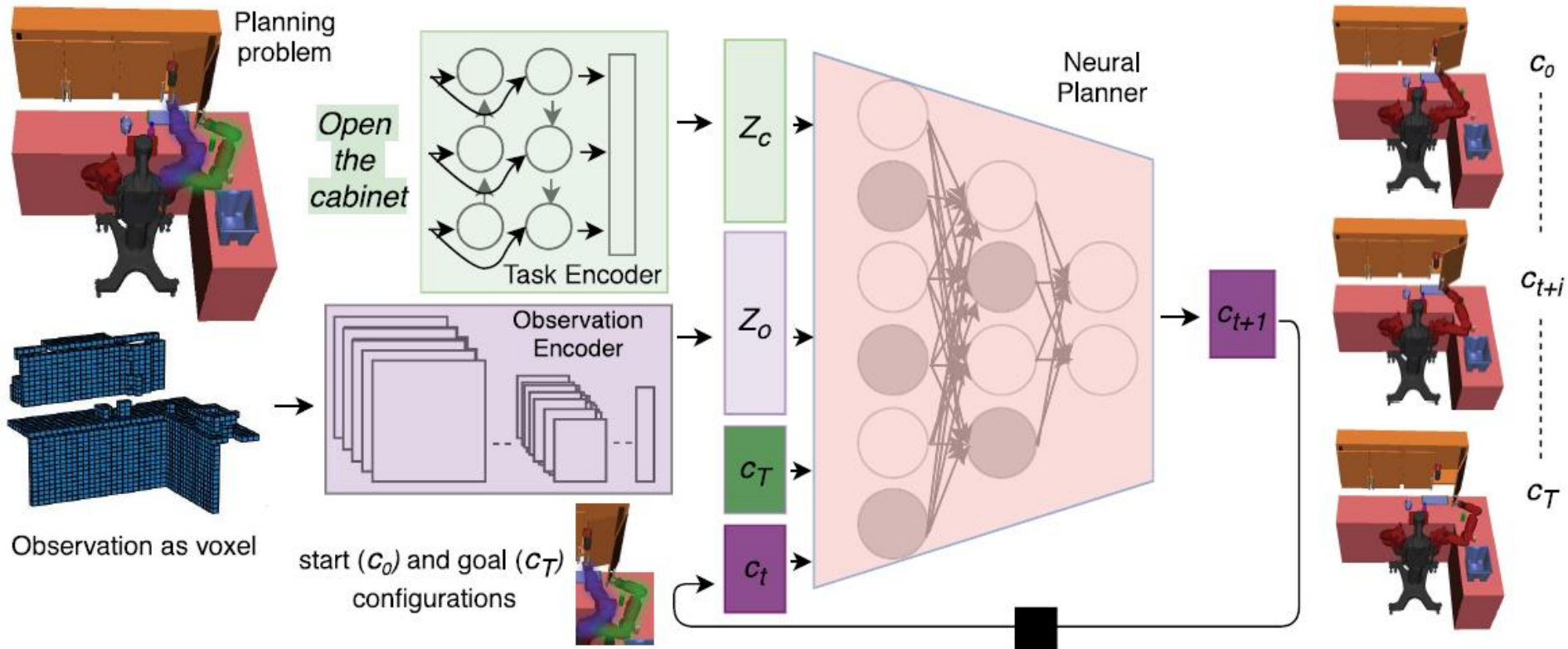
Atlas



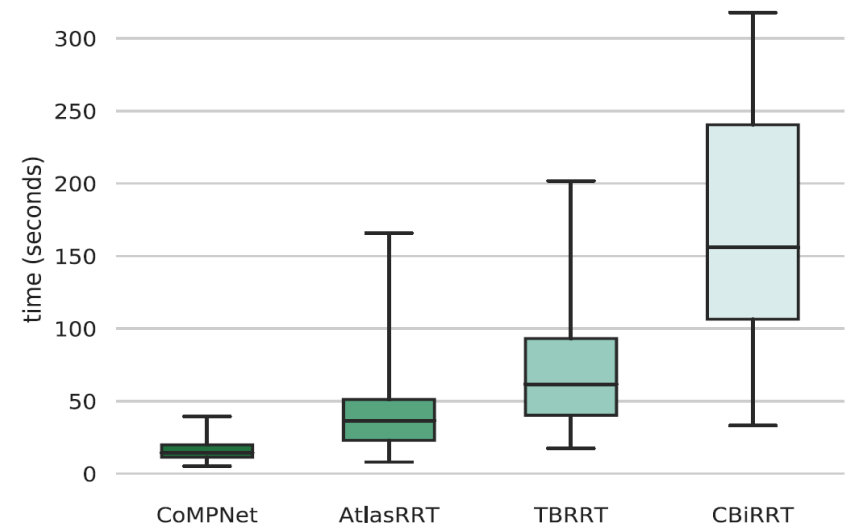
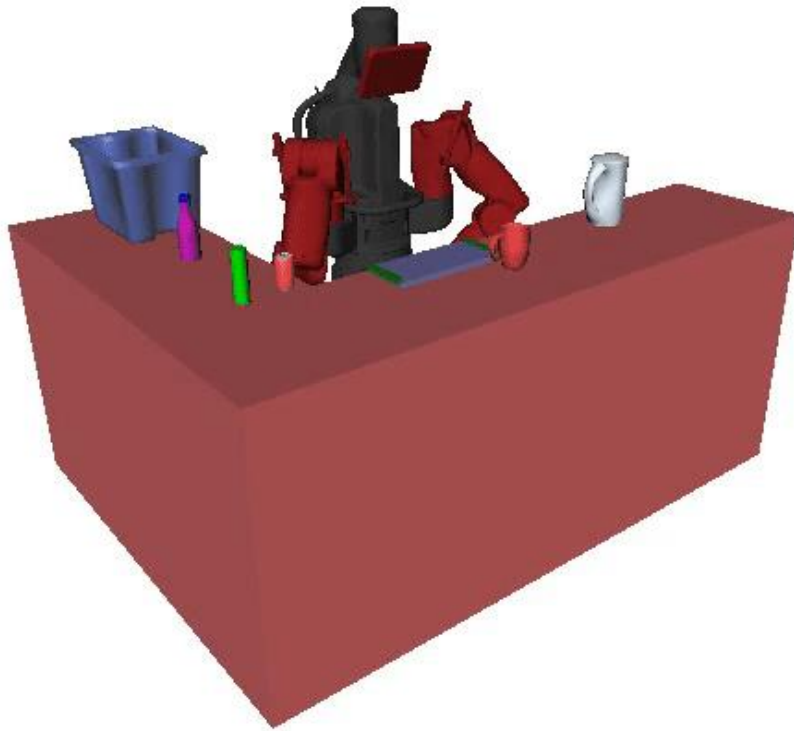
Tangent Bundle

- [1] Berenson et. al. (2011). Task space regions: A framework for pose-constrained manipulation planning, *IJRR*.  
[2] Jaillet & Porta (2012). Path planning under kinematic constraints by rapidly exploring manifolds. *IEEE TRO*.  
[3] Kim et. al. (2016). Tangent bundle RRT: A randomized algorithm for constrained motion planning. *Robotica*.

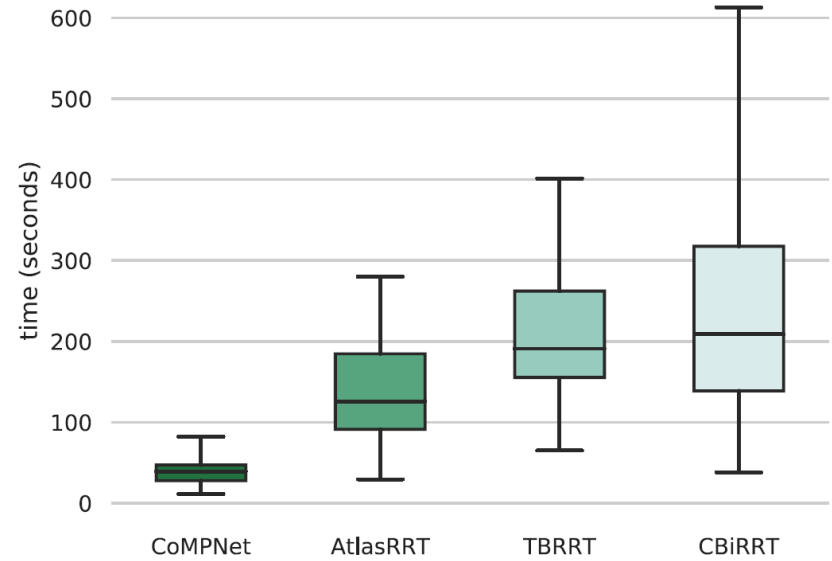
# Constrained Motion Planning Networks



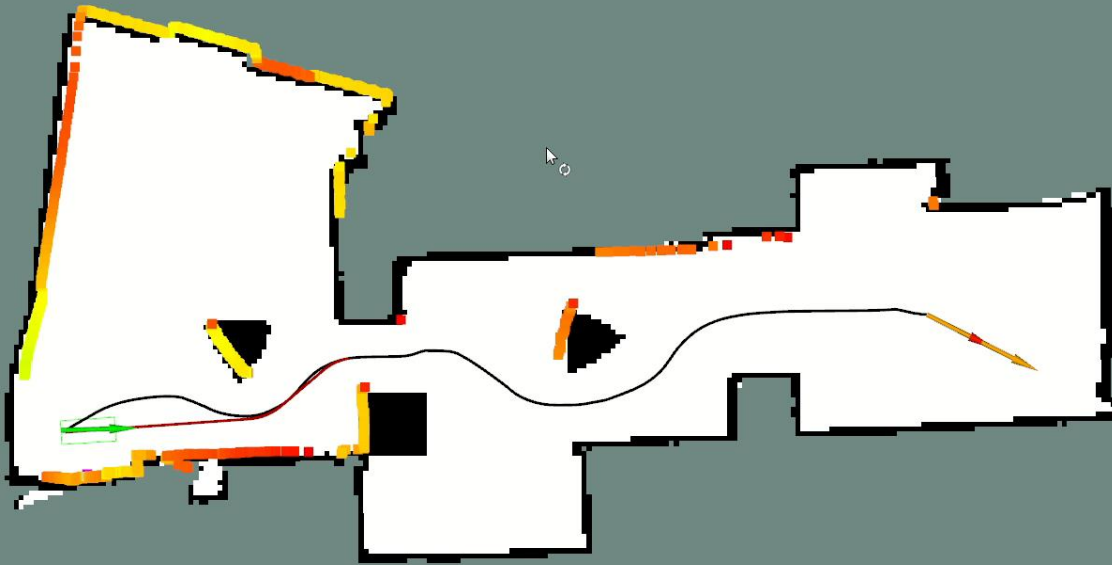
# CoMPNet: Results



# CoMPNet: Results



# Dynamically Constrained Motion Planning Networks



Jacob Johnson

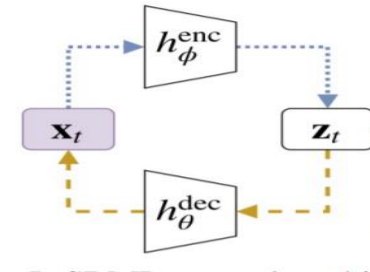


- Real-time planning with egocentric maps
- Generates samples that satisfy non-holonomic constraints
- Provide local planner plugin for ROS navigation stack
  - [https://github.com/jacobjj/mpnet\\_local\\_planner](https://github.com/jacobjj/mpnet_local_planner)

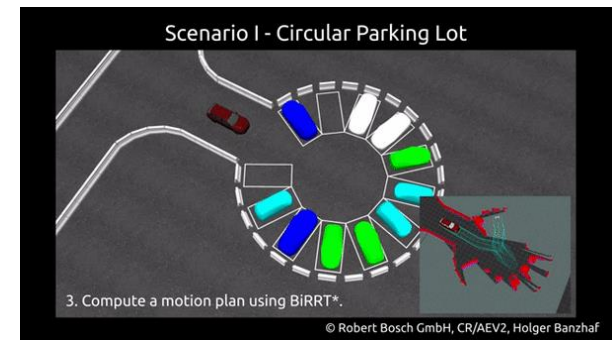
J. Johnson et. al, *Dynamically Constrained Motion Planning Networks for Non-Holonomic Robots*, IROS2020.

# Extensions to Motion Planning Networks / Neural Planning

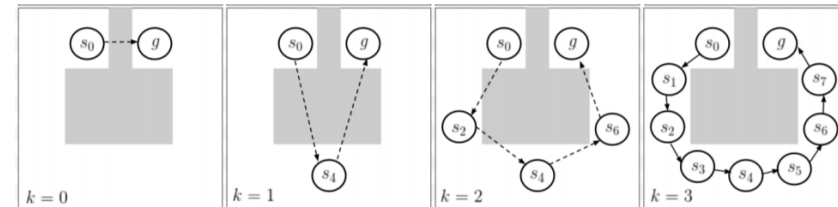
- **Planning in Learned Latent Spaces** –  
*Ichter and Pavone. RAL 4.3 (2019): 2407-2414.*



- **Sampling-based ego-poses for planning motions of nonholonomic vehicles** –  
*Banzhaf, et al. RAL 4.2 (2019): 1053-1060.*



- **Subgoal Trees** – Jurgenson, Groshev, Tamar." *ICML (2019).*



- **Harnessing Reinforcement Learning for Neural Motion Planning** – Jurgenson, Tamar." *RSS (2019).*



# Publications

[1] **A.H.Qureshi**, Y.Miao, A.Simeonov, and M.C.Yip. “Motion Planning Networks: Bridging the Gap Between Learning-based and Classical Motion Planners”, *IEEE Transactions on Robotics (TRO)*, 2020.

[3] **A.H.Qureshi**, A.Simeonov, M.J.Bency, M.C.Yip. “Motion Planning Networks”, *IEEE/RAS International Conference on Robotics and Automation (ICRA)*, pp. 2118-2124, Montreal, Canada 2019.

[4] **A.H.Qureshi** and Michael.C.Yip . “Deeply Informed Neural Sampling For Robot Motion Planning”, *Proceedings of IEEE/RSJ International Conference on Intelligent Robot and Systems (IROS)*, pp. 6582-6588, Madrid, Spain 2018.

[5] **A.H.Qureshi**, J.Dong, A.Cho, and M.C.Yip. “Neural Manipulation Planning on Constraints Manifolds”, *IEEE Robotics and Automation Letters (RAL)*, 2020.

[5] J.Johnson, L.Jun, F.Liu, **A.H.Qureshi** and M.C.Yip. “Dynamically Constrained Motion Planning Networks for Non-Holonomic Robots”, *IEEE IROS*, 2020.



ANY  
QUESTIONS?

A hand holding a piece of white chalk is pointing towards the question mark at the end of the text 'ANY QUESTIONS?'. The text is written in a light, textured font on a dark background.

**THANK YOU**